## Sequence sensitivity of breathing dynamics in heteropolymer DNA

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We study the fluctuation dynamics of localized denaturation bubbles in heteropolymer DNA with a master equation and complementary stochastic simulation based on novel DNA stability data. A significant dependence of opening probability and waiting time between bubble events on the local DNA sequence is revealed and quantified for a biological sequence of the T7 bacteriophage. Quantitative agreement with data from fluorescence correlation spectroscopy (FCS) is demonstrated.

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The biological function of DNA largely relies on its physical properties: Protein binding is sensitive to local DNA structure [1], DNA looping facilitates the search of binding proteins for their specific site [2], and DNA knots impair transcription or act as barriers between different genome regions [3]. Similarly, local denaturation of DNA is necessary for protein binding to DNA singlestrand [4, 5, 6], and is implicated in transcription initiation [7, 8]. DNA melting has a long tradition in statistical physics [9]. Its biological relevance is due to the fact that the free energy for breaking a single base pair (bp) at physiological temperature is  $\sim k_B T$  [10, 11]. Renewed interest in DNA melting, from a physics perspective is nourished by the possibility to measure the fluctuation dynamics of local denaturation bubbles by single molecule FCS [12].

We present a master equation (ME) and complementary stochastic simulation, that provides the time series of the bubble fluctuations. A full two-variable formulation in terms of bubble size m and left fork location  $x_L$  allows to investigate an arbitrary sequence of bps, beyond previous homopolymer [5] and random energy models [13]. In certain limits, the ME can be solved analytically. We employ DNA stability data from a novel approach measuring the ten stacking interactions separately and, inter alia predicting a distinct asymmetry between AT/AT and AT/TA nearest neighbour bps [11]. As proved on recent FCS experimental data our model describes well the bubble dynamics with only one free parameter. We demonstrate the delicate sensitivity of bubble dynamics to the local sequence of heterogeneous DNA on the promoter sequence of the T7 bacteriophage, and illustrate good potential for nanosensor applications.

Model. With typical experimental setups [12] in mind, we consider a segment of double-stranded DNA with M internal bps, that are clamped at both ends (Fig. 1). The full sequence of bps enters via the position-dependence of the statistical weights  $u_{\rm hb}(x) = \exp\{\epsilon_{\rm hb}(x)/[k_BT]\}$  for breaking the hydrogen-bonds of the bp at position x, and  $u_{\rm st}(x) = \exp\{\epsilon_{\rm st}(x)/[k_BT]\}$  for disrupting the stacking interactions between bps x-1 and x. Due to the high free energy barrier for bubble initiation ( $\xi \ll 1$ ), opening and

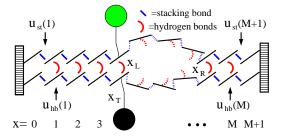


FIG. 1: Clamped bubble domain with internal bps x = 1 to M, statistical weights  $u_{\text{hb}}(x)$ ,  $u_{\text{st}}(x)$ , and tag position  $x_T$ .

merging of multiple bubbles are rare events, such that a one-bubble description is appropriate. The positions  $x_L$  and  $x_R$  of the zipper forks correspond to the right-and leftmost closed bp of the bubble.  $x_L$  and  $x_R$  are stochastic variables, whose time evolution in the energy landscape defined by the partition factor  $(m \ge 1)$ 

$$\mathscr{Z}(x_L, m) = \frac{\xi'}{(1+m)^c} \prod_{x=x_L+1}^{x_L+m} u_{\text{hb}}(x) \prod_{x=x_L+1}^{x_L+m+1} u_{\text{st}}(x) \quad (1)$$

characterizes the bubble dynamics.  $\mathscr{Z}$  is written in terms of  $x_L$  and bubble size  $m=x_R-x_L-1$ , with  $\mathscr{Z}(m=0)=1$ . Here,  $\xi'=2^c\xi$ , where  $\xi\approx 10^{-3}$  is the ring factor for bubble initiation from Ref. [11] that is related to the cooperativity parameter  $\sigma_0\approx 10^{-5}$  [9, 10] by  $\sigma_0=\xi\exp\{\epsilon_{\rm st}\}$  [11]. For the entropy loss on forming a closed polymer loop we assign the factor  $(1+m)^{-c}$  [10, 14] and take c=1.76 for the critical exponent [15]. Note that a bubble with m open bps requires breaking of m hydrogen bonds and m+1 stacking interactions.

The zipper forks move stepwise  $x_{L/R} \to x_{L/R} \pm 1$  with rates  $\mathfrak{t}_{L/R}^{\pm}(x_L, m)$ . We define for bubble size decrease

$$\mathsf{t}_L^+(x_L, m) = \mathsf{t}_R^-(x_L, m) = k/2 \qquad (m \ge 2)$$
 (2)

for the two forks [16]. The rate k characterizes a single bp zipping. Its independence of x corresponds to the view that bp closure requires the diffusional encounter of the two bases and bond formation; as sterically AT and

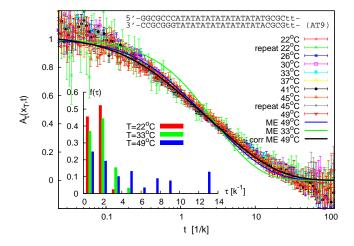


FIG. 2: Scaling plot of  $A_t(x_T, t)$  at various T for the sequence AT9 from [12]. Inset: Relaxation time spectrum. See text.

GC bps are very similar, k should not significantly vary with bp stacking. k is the only adjustable parameter of our model, and has to be determined from experiment or future MD simulations. The factor 1/2 is introduced for consistency [5]. Bubble size increase is controlled by

$$t_L^-(x_L, m) = k u_{\rm st}(x_L) u_{\rm hb}(x_L) s(m)/2,$$
  
 $t_R^+(x_L, m) = k u_{\rm st}(x_R + 1) u_{\rm hb}(x_R) s(m)/2,$  (3)

for  $m \ge 1$ , where  $s(m) = \{(1+m)/(2+m)\}^c$ . Finally, bubble initiation and annihilation from and to the zero-bubble ground state,  $m = 0 \leftrightarrow 1$  occur with rates

$$t_G^+(x_L) = k\xi' s(0)u_{\rm st}(x_L+1)u_{\rm hb}(x_L+1)u_{\rm st}(x_L+2)$$
  

$$t_G^-(x_L) = k.$$
(4)

The rates t fulfill detailed balance conditions. The annihilation rate  $\mathsf{t}_G^-(x_L)$  is twice the zipping rate of a single fork, since the last open bp can close either from the left or right. Due to the clamping,  $x_L \geq 0$  and  $x_R \leq M+1$ , ensured by reflecting conditions  $\mathsf{t}_L^-(0,m) = \mathsf{t}_R^+(x_L, M-x_L) = 0$ . The rates t together with the boundary conditions fully determine the bubble dynamics.

In the FCS experiment fluorescence occurs if the bps in a  $\Delta$ -neighbourhood of the fluorophore position  $x_T$  are open [12]. Measured fluorescence time series thus correspond to the stochastic variable I(t), that takes the value 1 if at least all bps in  $[x_T - \Delta, x_T + \Delta]$  are open, else it is 0. The time averaged  $(\overline{\cdot})$  fluorescence autocorrelation

$$A_t(x_T, t) = \overline{I(t)I(0)} - \overline{I(t)}^2$$
 (5)

for the sequence AT9 from [12] are rescaled in Fig. 2 [17]. ME. DNA breathing is described by the probability distribution  $P(x_L, m, t)$  to find a bubble of size m located at  $x_L$  whose time evolution follows the ME

 $\partial P(x_L,m,t)/\partial t=\mathbb{W}P(x_L,m,t).$  The transfer matrix  $\mathbb{W}$  incorporates the rates t. Detailed balance guarantees equilibration toward  $\lim_{t\to\infty}P(x_L,m,t)=\mathcal{Z}(x_L,m)/\mathcal{Z},$  with  $\mathcal{Z}=\sum_{x_L,m}\mathcal{Z}(x_L,m)$  [5, 18]. The ME and the explicit construction of  $\mathbb{W}$  are discussed at length in Refs. [5, 19]. Eigenmode analysis and matrix diagonalization produces all quantities of interest such as the ensemble averaged autocorrelation function

$$A(x_T, t) = \langle I(t)I(0)\rangle - (\langle I\rangle)^2. \tag{6}$$

 $\langle I(t)I(0)\rangle$  is proportional to the survival density that the bp is open at t and that it was open initially [5, 19].

In Fig. 2 the blue curve shows the predicted behaviour of  $A(x_T, t)$ , calculated for  $T = 49^{\circ}$ C with the parameters from [11]. As in the experiment we assumed that fluorophore and quencher attach to bps  $x_T$  and  $x_T + 1$ , that both are required open to produce a fluorescence signal. From the scaling plot, we calibrate the zipping rate as  $k = 7.1 \times 10^4/\text{s}$ , in good agreement with the findings from Ref. [12, 20]. The calculated behaviour reproduces the data within the error bars, while the model prediction at  $T = 35^{\circ}\text{C}$  shows more pronounced deviation. Potential causes are destabilizing effects of the fluorophore and quencher, and additional modes that broaden the decay of the autocorrelation. The latter is underlined by the fact that for lower temperatures the relaxation time distribution  $f(\tau)$ , defined by  $A(x_T,t) =$  $\int \exp(-t/\tau) f(\tau) d\tau$ , becomes narrower (Fig. 2 inset). Deviations may also be associated with the correction for diffusional motion of the DNA construct, measured without quencher and neglecting contributions from internal dynamics [21]. Indeed, the black curve shown in Fig. 2 was obtained by a 3% reduction of the diffusion time [22]; see details in [19].

Stochastic simulation. Based on the rates t, stochastic simulations give access to single bubble fluctuations [19, 23]. Our customized Gillespie algorithm uses the joint probability density of waiting time  $\tau$  and path  $\mu = +/-$ ,

$$P(\tau, \mu, \nu) = \mathsf{t}^{\mu}_{\nu}(x_L, m) \exp\left(-\tau \sum_{\mu, \nu} \mathsf{t}^{\mu}_{\nu}(x_L, m)\right), \quad (7)$$

defining for given state  $(x_L, m)$  after what time  $\tau$  the next step of fork  $\nu \in \{L, R\}$  occurs. The formulation via the waiting time density  $\sum_{\mu,\nu} P$  is economical computationally, avoiding a large number of unsuccessful opening attempts in traditional Langevin simulations. Using (7) we obtain the single bubble time series in Fig. 3.

Phage T7 analysis. By ME and stochastic simulation we investigate the promoter sequence of the T7 phage,

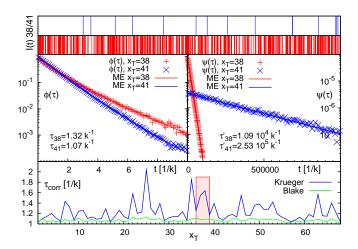


FIG. 3: Time series I(t) for the T7 promoter, with  $x_T = 38$ , 41. Middle: Waiting time  $(\psi(\tau))$  and fluorescence time  $(\phi(\tau))$  densities. Bottom: Mean fluorescence time for  $\Delta = 0$ .

whose TATA motif is marked red [8]. Fig. 3 shows the time series of I(t) at 37°C for the tag positions  $x_T = 38$ in the core of TATA, and  $x_T = 41$  at the second GC bp after TATA: Bubble events occur much more frequently in TATA (AT/TA bps are particularly weak [11]). This is quantified by the density of waiting times  $\psi(\tau)$  in the I=0 state, whose characteristic time scale  $\tau'$  is more than an order of magnitude longer at  $x_T = 41$ . In contrast, we observe similar behaviour for the density  $\phi(\tau)$  in the I=1 state for  $x_T=38$  and 41. Both  $\psi(\tau)$  and  $\phi(\tau)$ decay exponentially for long t; the overlaid lines represent numerical evaluation of the ME, see [19]. As shown in the bottom for the parameters from [11], the variation of the mean correlation time  $\tau_{\rm corr} = \int A(x_T, t) dt$  obtained from the ME is small for the entire sequence, consistent with the low sequence sensitivity of  $\phi(\tau)$ . Note the even smaller variation predicted for the parameters of [10].

Fig. 4 shows the equilibrium probability that the bps  $[x_T - \Delta, x_T + \Delta]$  are open, as necessary for fluorescence to occur. We plot data obtained from the zeroth mode of the ME together with the time average from the Gillespie algorithm (GA), finding excellent agreement. Whereas for  $\Delta = 0$  several segments show increased tendency to opening, for the case  $\Delta = 2$ , one major peak is observed; the data from [11] coincide precisely with TATA, while the data from [10] peak upstream. Also shown is a comparison to the opening probability of a random sequence demonstrating that the enhanced opening probability at TATA is significant, compare [19]. Analysis for various  $\Delta$  indicate best discrimination of the TATA sequence being open for  $\Delta = 2$ . For future FCS or energy transfer experiments, it therefore appears important to optimise the  $\Delta$ -dependence for best resolution, e.g., by adjusting the linker lengths of fluorophore and quencher [25].

Nanosensing. Fig. 5 shows the dependence of the mean

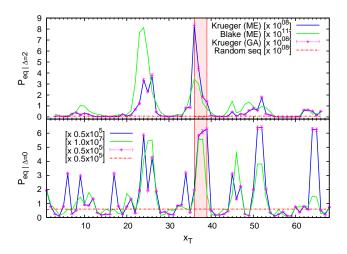


FIG. 4: Probability to have bps  $[x_T - \Delta, x_T + \Delta]$  open.

correlation time of the AT9 sequence on salt concentration C and T. The variation with C and T is significant, pointing toward potential applications of DNA fluorescence constructs as nanosensors [24]. The triangles denote the melting concentration of infinitely long random AT and GC stretches, respectively (see [11]). The maxima of the  $\tau_{\rm corr}$  curves hallmark the critical slowing down of the autocorrelation at the phase transition point beyond which the bubble is preferentially open, see also [26]. Note that the maxima coincide with the melting concentrations in the bottom panel. The dashed line  $(\tau_{\text{max}} 2D)$ corresponds to the longest relaxation time obtained numerically from the ME; it agrees well with  $\tau_{\rm corr}$  close to the maximum, analogously for the other T. The horizontal line ( $\tau_{\rm max}$  1D) represents the longest relaxation time  $(2M+1)^2/\pi^2k^{-1}$  obtained from the homopolymer model of Ref. [5] in the limit  $u \to 1$ ,  $\sigma_0 \to 0$  and c = 1 (M = 27, length of the AT9 construct), with the same scaling as the first exit of unbiased diffusion.

Discussion. Previous bulk melting studies provided DNA stability data [10, 11], on whose basis the relation between local sequence stability and coding properties of the associated genes was shown [7, 27]. However, it is single molecule experiments that permit to study the dynamics of DNA denaturation and renaturation [12]. We here derive a physical framework for the opening and closing fluctuations of intermittent DNA bubbles in an arbitrary sequence of bps using the position of the two bubble zipper forks as fundamental coordinates. By comparison with previously unpublished FCS data we prove the predictive power of our model. As complementary approach based on the same (un)zipping rates, we introduced the stochastic Gillespie simulation, that provides the time series of single bubble fluctuations. The time averages from the stochastic simulation agree well with the ensemble properties derived from the ME. By

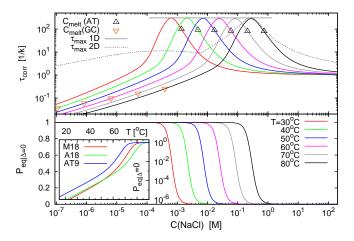


FIG. 5: Mean correlation time versus salt for various T (top), and melting curves versus salt concentration and T (bottom).

its computationally attractive formulation based on the waiting time the Gillespie approach allows to include additional effects such as protein binding dynamics, or to consider longer chains and multibubble states. For a long homopolymer our model is analytically tractable [5, 19].

We used recent DNA stability data from [11] based on separation of hydrogen bond and stacking energies, a distinct feature being the low stacking in a TA/AT stack, translating into a pronounced instability of the TATA motif, as shown for the T7 promoter sequence. The relevance of stacking interactions is also shown in the inset in Fig. 5 exhibiting pronouncedly different melting behaviour despite identical AT and GC contents for the constructs in [12, 28]. Regarding the biological relevance of TATA, from our analysis it may be speculated that it is not primarily the bubble lifetime (typically shorter than the timescale of protein conformational changes) but the recurrence frequency of bubble events that triggers the initiation of transcription. Note that typical binding energies of TATA binding proteins exceed the free energy to break up TATA, while both energies are comparable for a random sequence of the same length.

Given the high sensitivity of bubble dynamics to the stability parameters it should be of interest to employ FCS on designed DNA constructs to more accurately obtain stability data for different DNA structures and to calibrate the (un)zipping rates.

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